# Social Security and Female Labor Supply in China 

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## Introduction

- Motivation: To maintain fiscal sustainability, the Chinese government plans to raise social security eligibility age
- current policy: 50 for women and 60 for men
- proposed: 60 for all
- Question: How will increasing women's social security eligibility age from 50 to 60 affect
- employment of women?
- women's occupational choice, human capital, and earnings?


## Fact 1: current social security policy characterizes employment rate of urban Chinese women


$\Longrightarrow$ Will the reform incentivize women above age 50 to continue working?

## Fact 2: sizable grandparental childcare contributes to labor supply of young women

- $80 \%$ women have grandchildren by age 60
- $30 \%$ grandparents provide childcare, on average $13 \mathrm{hrs} /$ week
- employment rate of women with children under 7 is on average $\mathbf{2 6}$ percentage points higher in households with the elderly than those without
$\Longrightarrow$ Will the reform bring unintended effects on young women'
labor supply?


## Fact 3: wage growth mostly occurs on early career path



Source: Urban Household Survey of China

- High-skilled: abstract task intensive (around $20 \%$ of employment)
- Low-skilled: routine or manual task intensive
$\Longrightarrow$ How will the reform affect women's occupational choice, human capital, \& earnings?


## What we do

This paper: policy effect of delaying retirement on women's employment \& human capital over the life cycle

- Model: dynamic female labor supply over life cycle, featuring
- voluntary retirement
- parental, grandparental and market formal child care
- occupational choice, human capital and wage dynamics
- Calibration: unique features of Chinese data to infer
- intergenerational time transfer: time allocation on child care for young \& old women
- human capital dynamics: employment \& wage growth by occ.


## What we find

human capital dynamics \& intergenerational time transfer are
key to

- matching benchmark life cycle employment \& wage growth
- understanding policy effects of delaying retirement
(1) moderate increase in aggregate labor supply
- women above age 50 increase labor supply
- low-skilled young women decrease labor supply
(2) persistent employment/human capital/earnings losses over life


## Related literature

- Social security reform in China : Song, Storesletten, Wang, \& Zilibotti (2015), İmrohoroğlu \& Zhao (2018), He, Ning, \& Zhu (2019), Deng, Fang, Hanewald, \& Wu (2021)

This paper: focus on women \& human capital

- Intergenerational time transfer: Feng \& Zhang (2018), Rupert \& Zanella (2018), Frimmel, Halla, Schmidpeter, \& Winter-Ebmer (2020)
- Human capital dynamics (of women): Keane and Wolpin (2007,2010), Eckstein, Keane, \& Lifshitz (2019), Blundell, Costa Dias, Meghir, \& Shaw (2016), Adda, Dustmann, \& Stevens (2017)

This paper: (1) unified life cycle framework motivated by unique data features of China (2) quantify roles of human capital dynamics and intergenerational time transfer in policy design

## Outline

## Quantitative Model

Implications

Policy Experiment

## Quantitative Model

## Model environment

- Overlapping generations:
- 2 genders $\times 2$ generations: $i$ individual, $j$ period
- stochastic arrival of children manifested as time costs
- pool monetary resources + jointly make decisions
- unitary preference: consumption, leisure, \& childcare


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- Government: linear income tax + social security
- voluntary retirement of women starting from age 50


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- pool monetary resources + jointly make decisions
- unitary preference: consumption, leisure, \& childcare
- Government: linear income tax + social security
- voluntary retirement of women starting from age 50
- Main features: intergenerational time transfer + dynamic human capital accumulation


## Time allocation

- Time endowment is 1 for each household member every period
- Individual time constraint: time on leisure ( $l$ ), child care ( $q$ ), and work ( $n$ )

$$
l^{i}+q^{i}+n^{i} \leq 1, \quad l^{i} \geq 0, \quad q^{i} \geq 0 \quad \forall i \in \mathcal{I}
$$

- non-retired women choose $\in\{0, \bar{n}\}$
- $n=\bar{n}$ for men, $n=0$ for retired


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- non-retired women choose $\in\{0, \bar{n}\}$
- $n=\bar{n}$ for men, $n=0$ for retired
- Child care time constraint: parental, grandparental, and formal child care hours to meet

$$
\sum_{i \in \mathcal{I}} q^{i}+q^{n} \geq \underbrace{\kappa_{\pi}}_{\text {time cost }}
$$

## Occupations, human capital, \& wages of women

- Occupational choice at the beginning of period 1 , household chooses occupation for young women

$$
k^{\mathrm{yf}}=\underset{k \in\{1,2\}}{\arg \max }\left\{V_{1}\left(a-\psi_{k}, \pi, \mathbf{s}\right)+\varepsilon_{k}\right\}
$$

- training cost $\psi_{k}+$ type I EV unobserved shocks $\varepsilon_{k}$
- occupation is fixed over the life cycle


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- training cost $\psi_{k}+$ type I EV unobserved shocks $\varepsilon_{k}$
- Choice probability
- occupation is fixed over the life cycle
- Human capital evaluation $h_{j=1}=1$

$$
h_{j+1}=(1+\rho(k, n, j)) h_{j} \text { with } \rho(k, n, j)= \begin{cases}e^{\rho_{k, 1}+\mathrm{j} \rho_{k, 2}} & \text { if } n_{j}=\bar{n} \\ \rho_{k, 0} & \text { otherwise }\end{cases}
$$

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$$

- Wage income occupation $(k)+$ human capital $(h)+\operatorname{shocks}(\epsilon)$


## Recursive formulation

- States $\mathbf{x}$ : assets $(a)$, children age $(\pi)$, incomes $\left(s^{i}\right)$
- Choices $\mathbf{d}=\left\{k^{\text {yf }}, r^{\text {of }}, \mathbf{n}, \mathbf{l}, \mathbf{q}, q^{n}, \mathbf{c}, a^{\prime}\right\}$

$$
\begin{array}{ll}
V_{j}(\mathbf{x})=\max _{\mathbf{d}}\left\{u(\mathbf{c}, \mathbf{l}, \mathbf{q})+\beta \mathbb{E}\left[\hat{V}_{j+1}\left(\mathbf{x}^{\prime}\right)\right]\right\} \\
\text { s.t. } & c^{y}+c^{o}+p^{n} q^{n}+a^{\prime}=(1+r) a+y_{j}\left(\mathbf{s},\left\{n^{i}\right\}_{i \in \mathcal{I}} ; \mathcal{T}\right) \\
& l^{i}+q^{i}+n^{i} \leq 1, \quad l^{i} \geq 0, \quad q^{i} \geq 0, \quad n^{i} \in\{0, \bar{n}\} \quad \forall i \in \mathcal{I} \\
& \sum_{i \in \mathcal{I}} q^{i}+q^{n} \geq \kappa_{\pi} \\
& a^{\prime}>\underline{a}
\end{array}
$$

with

$$
\hat{V}_{j+1}\left(\mathbf{x}^{\prime}\right)= \begin{cases}V_{j+1}\left(\mathbf{x}^{\prime}\right) & \text { for } j=1, \ldots, 11 \\ \max _{k^{\mathrm{y}} \in\{1, \ldots, K\}}\left\{V_{1}\left(a^{\prime}-\psi_{k}, \pi^{\prime}, \mathbf{s}^{\prime}\right)+\varepsilon_{k}\right\} & \text { for } j=12\end{cases}
$$

## Implications

## Role of grandparental child care



- Blue: fitness of benchmark model
- Red: fix all params to benchmark + shut down grandparental care $\Longrightarrow$ size of grandparental care


## Role of age-dependent human capital growth



- Constant wage growth reduces opportunity cost of non-employment for young women $\Longrightarrow$ employment rate of young $\downarrow$

Policy Experiment

## Experiments

## Policy counterfactual

- raise social security eligibility age of women from 50 to 60
- adjust income tax to balance the government budget
- compare allocations at steady states

|  | Baseline | Counterfactual |
| :--- | :---: | :---: |
| SS. entitlement age of women | 50 | 60 |
| Income tax rate | 0.28 | 0.23 |
| Share choosing high-skilled occ. | $25 \%$ | $32 \%$ |

## Policy impacts



- High-skilled
- barely change before 50
- Low-skilled
- large and persistent drop before 50
- Both increase after 50

Employment by occupation

## Policy impacts



Employment by occupation


Lifetime By age 40
Total working years $\quad+3.1 \quad-1.0$

## Robustness

- Population aging
- Alternative entitlement ages
- Formal childcare supply


## Concluding remarks: implications for SS reform

- Results: delaying SS entitlement of women in China
- increases labor supply of old but reduces labor supply of young
- persistent employment/human capital loss
- Key features
- intergenerational time transfer
- dynamic human capital accumulation
- Potential accompany policy tools
- child care subsidies
- training subsidies


## Appendix

Female Labor Supply in China

Child care Time Allocation

Model

Calibration

Policy Experiment

Female Labor Supply in China

Lifecycle employment status by gender


Age distribution of retirement in urban China


Weekly Hours of Urban Employment by Gender and Age


## Weekly hours distribution for women with children

| Age | Obs. | emp. | hours | $<10 h$ | $<20 h$ | mean | p25 | median | p75 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $25-29$ | 89 | $80 \%$ | $94 \%$ | $3.0 \%$ | $3.0 \%$ | 42 | 39 | 41 | 55 |
| $30-35$ | 193 | $86 \%$ | $100 \%$ | $0 \%$ | $0 \%$ | 43 | 41 | 41 | 55 |
| $35-39$ | 311 | $86 \%$ | $97 \%$ | $0 \%$ | $2.7 \%$ | 43 | 41 | 41 | 55 |
| $40-44$ | 330 | $84 \%$ | $98 \%$ | $0.4 \%$ | $2.2 \%$ | 44 | 41 | 41 | 55 |
| $45-49$ | 85 | $78 \%$ | $100 \%$ | $1.5 \%$ | $3.0 \%$ | 46 | 41 | 43 | 65 |

Table: Weekly working hours of urban employed mothers, with children under age 18.
Source: China Household Income Project 2013

Child care Time Allocation

## Age profile of grandchildren in overall economy



## Childcare in the CTUS

- sample size: 19621 individuals from 9049 households, 10 provinces;
- Variables include:
- primary activity code, secondary activity code, time length of activity, transportation method to conduct activity, other people present when conducting activity
- age, relationship to the head, marital status, education and employment status
- Assign couples both above age 50 as grandparents


## - Imputation errors

- Construction of
- extensive margin: probability of providing positive childcare hours conditional on being grandparents
- intensive margin: childcare hours conditional on providing positive hours


## Childcare activities in CTUS 2008

| Code | Activity | Descriprition |
| :--- | :--- | :--- |
| 611 | Physical or daily life care | dressing, feeding, bathing <br> children, medical activities <br> for children <br> teaching children, reading <br> for children, chatting or <br> playing with children <br> watching children when <br> children are playing <br> taking children to public, <br> such as amusement park, <br> hospital, or school |
| 613 | Educational care Looking after children | Activities out of household |

Table: Categories of Childcare Activities

## Grandparental childcare in CTUS 2008

| Age | Men |  | Women |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Employed | Retired | Employed | Retired |
| Panel A: weekly child care hours |  |  |  |  |
| 50-54 | 6.56 | - | 8.01 | 17.84 |
| 55-59 | 8.29 | - | 7.67 | 15.00 |
| 60-64 | - | 11.01 | - | 13.26 |
| 65-70 | - | 8.36 | - | 9.71 |
| Panel B: fraction of child care provision |  |  |  |  |
| 50-54 | 0.14 | - | 0.22 | 0.39 |
| 55-59 | 0.21 | - | 0.23 | 0.41 |
| 60-64 | - | 0.38 | - | 0.30 |
| 65-70 | - | 0.23 | - | 0.20 |

Model

## Households

- Overlapping generations
- Life starts at age 22
- Individual goes through the young and old stages sequentially
- Generations overlapped for 24 years (12 model periods)
- Children are manifested as time cost to the household
- Household structure: two generations $\times$ two genders

$$
i \in \mathcal{I}=\{\mathrm{ym}, \mathrm{yf}, \mathrm{om}, \mathrm{of}\}
$$

- Household members jointly make decisions


## Household decision problem: states

States of the household: $\mathbf{x}=(a, \pi, \mathbf{s})$

- assets: $a$
- children age: $\pi$
- income-related state variables: $\mathbf{s}=\left\{s^{i}\right\}_{i \in \mathcal{I}}$ including
- $k^{i}$ : occupation
- $h^{i}$ : human capital
- $\epsilon^{i}$ : income shock
- $r^{i}$ : retirement status
- $z^{i}$ : average lifetime earnings

Household decision problem: choices \& preference

- Choices: $\mathbf{d}=\left\{k^{\mathrm{yf}}, r^{\mathrm{of}}, \mathbf{n}, \mathbf{l}, \mathbf{q}, q^{n}, \mathbf{c}, a^{\prime}\right\}$
- occupation of young women: $k^{\text {yf }} \in\{1, \ldots, K\}$
- retirement of old women: $r^{\text {of }} \in\{0,1\}$
- working hours: $\mathbf{n}=\left\{n^{i}\right\}_{i \in \mathcal{I}}$
- leisure: $\mathbf{l}=\left\{l^{i}\right\}_{i \in \mathcal{I}}$
- household members' childcare hours: $\mathbf{q}=\left\{q^{i}\right\}_{i \in \mathcal{I}}$
- market formal childcare hours: $q^{n}$
- consumption of young and old generation: $\mathbf{c}=\left\{c^{y}, c^{o}\right\}$
- assets: $a^{\prime}$
- Period utility of household: $u(\mathbf{c}, \mathbf{l}, \mathbf{q})$


## Demographics

Fertility shocks: stochastic arrival of children such that

- all households have children once \& before age 40 of the young generation
- take care of children for 16 years

Mortality shocks:

- common to the old generation in the household


## Government

Government policy tools $\mathcal{T}$ include:

- Linear wage income tax: $\tau$
- Social security: $b(z)$
- social security eligibility age is 50 for women and 60 for men
- all individuals retire by age 60
- no rehiring after retirement
- Exogenous government spending $G$
- Government budget balanced

$$
\tau \sum_{i} w^{i} \mathbb{1}_{\left\{n^{i}=\bar{n}\right\}}-\sum_{i} b\left(z^{i}\right) \mathbb{1}_{\left\{r^{i}=1\right\}}-G=0
$$

## Occupational choice probability

- Denote value function conditional on the choice of occupation $k^{\mathrm{yf}}=v$

$$
\mathrm{EV}_{k}(\mathbf{x}, \pi, a)=V_{1}\left(a-\psi_{k}, \pi, \mathbf{s}\right)
$$

- Unobserved shock $\varepsilon_{k}$ follows type I extreme value distribution
- mean zero
- variance $\sigma_{e}^{2}$
- Probability of choosing occupation $v$ :

$$
\mathbb{P}\left(k^{\mathrm{yf}}=v\right)=\frac{\exp \left(\mathrm{EV}_{v} / \sigma_{e}\right)}{\sum_{k=1, \ldots, K} \exp \left(\mathrm{EV}_{k} / \sigma_{e}\right)}
$$

## Taking F.O.C (1)

- Consider the problem after employment choices are made $\bar{V}_{j}$,given expected value functions
- Denote the available time $t^{i}=1-h^{i}$ as the time endowment net working time

$$
\begin{array}{ll}
\bar{V}_{j}(\mathbf{x})=\max _{\mathbf{d}}\left\{u(\mathbf{c}, \mathbf{l}, \mathbf{q})+\beta \mathbb{E} V_{j+1}\left(\mathbf{x}^{\prime}\right)\right\} \\
\text { st. } & l^{i}+q^{i} \leq t^{i} \quad \forall i \in \mathcal{I} \\
& q^{y m}+q^{y f}+q^{o m}+q^{o f}+q^{n} \geq \kappa_{\pi} \\
& c^{y}+c^{o}+p^{n} q^{n}+a^{\prime}=(1+r) a+y_{j}  \tag{6}\\
& a^{\prime}>\underline{a} \\
& l^{i} \geq 0, \quad q^{i} \geq 0 \quad \forall i \in \mathcal{I}
\end{array}
$$

## Taking F.O.C (2)

F.O.C's are given as (for the ease of notation, denote $\{y f, y m, o f, o m\}$ as individuals $1,2,3,4$ )

$$
\begin{array}{lll}
\left(c^{y}\right) & \lambda_{6}=U_{c}^{y} & \\
\left(c^{o}\right) & \lambda_{6}=U_{c}^{o} & \\
\left(q^{n}\right) & \lambda_{6} p^{n}=\lambda_{5} & \\
\left(l^{i}\right) & \lambda_{i}=U_{l}^{i} & \forall i \in\{1,2,3,4\} \\
\left(q^{i}\right) & \lambda_{i}=U_{q}^{i}+\lambda_{5} & \forall i \in\{1,2,3,4\}
\end{array}
$$

it thus follows

$$
U_{l}^{1}=U_{q}^{1}+\lambda_{5}, \quad U_{l}^{2}=U_{q}^{2}+\lambda_{5}
$$

note that

$$
U_{l}^{1}=\left(l_{1}+\omega q_{1}\right)^{\rho-1} \frac{1}{2} H_{1}^{-\frac{1}{2}} H_{2}^{\frac{1}{2}} \frac{\left(c^{1-\nu} H^{\nu}\right)^{-\gamma}(1-\nu)}{H} \quad \text { and } \quad U_{q}^{1}=\omega U_{l}^{1}
$$

## Taking F.O.C (3)

By

$$
U_{l}^{1}=U_{q}^{1}+\lambda_{5} ; \quad U_{l}^{2}=U_{q}^{2}+\lambda_{5}
$$

note that

$$
\begin{array}{ll}
U_{l}^{1}=\frac{1}{2} H_{1}^{-\frac{1}{2}} H_{2}^{\frac{1}{2}} \frac{\left(c^{1-\nu} H^{\nu}\right)^{-\gamma}(1-\nu)}{H} ; & U_{q}^{1}=\omega U_{l}^{1} \\
U_{l}^{2}=\frac{1}{2} H_{2}^{-\frac{1}{2}} H_{1}^{\frac{1}{2}} \frac{\left(c^{1-\nu} H^{\nu}\right)^{-\gamma}(1-\nu)}{H} ; & U_{q}^{2}=\omega U_{l}^{2}
\end{array}
$$

we can get

$$
1=\frac{U_{l}^{2}}{U_{l}^{1}}=\frac{H_{1}}{H_{2}}=\frac{l_{1}+\omega q_{1}}{l_{2}+\omega q_{2}}=\frac{l_{1}+\omega\left(t_{1}-l_{1}\right)}{l_{2}+\omega\left(t_{2}-l_{2}\right)}
$$

thus

$$
t_{1}-t_{2}=(1-\omega)\left(q_{1}-q_{2}\right)
$$

## Calibration

## Calibration overview

## Data:

- Labor market: Urban Household Survey of China 2002-2009
- two occupations
- moments on employment and wages by occupation
- Time use: China Time Use Survey - 2008
- moments on childcare hours from the young and the old

Estimation: method of simulated moments

## Predetermined parameters

| Parameter | Value | Description |
| :---: | ---: | :--- |
| $r$ | 0.10 | Interest rate |
| $\beta$ | 0.90 | Discounting factor |
| $\gamma$ | 1.5 | Risk aversion |
| $R_{1}$ | 2 | Social security eligibility age of women: 50 |
| $\tau^{b}$ | 0.75 | Social security replacement ratio |
| $\tau$ | 0.28 | Income tax rate |
| $\bar{n}$ | 0.33 | Working time: $8 \mathrm{hr} /$ day |
| $\kappa_{1}$ | 0.42 | Childcare time for child $<7: 10 \mathrm{hr} /$ day |
| $\kappa_{2}$ | 0.08 | Childcare time for child $\geq 7: 2 \mathrm{hr} /$ day |

- Fertility and mortality shocks: Population Census
- Wage process of men: UHS


## Internal parameters

14 parameters:
(1) Preference parameters: $\left\{\nu, \omega^{y}, \omega^{o}\right\}$
(2) Childcare price: $p^{n}$
(3) Training cost for high-skilled occupation: $\psi_{2}$
(4) Standard deviation of unobserved shock: $\sigma_{e}$
(5) Occupation-specific human capital evolution:

$$
\left\{\rho_{k, 0}, \rho_{k, 1}, \rho_{k, 2}\right\}_{k \in\{1,2\}}
$$

(6) Occupational wage premium: $\left\{\alpha_{k}\right\}_{k \in\{1,2\}}$

## Internal parameters

| Par. | Description | Value | Targeted Moments | Data | Model |
| :--- | :--- | :--- | :--- | :---: | :---: |
|  |  |  |  |  |  |
| Preference \& childcare price |  |  |  |  |  |
|  |  |  |  |  |  |
| $\nu$ | Intensity of leisure | 0.42 | Employment rate under 50 | 18 | 18 |
| $\omega^{y}$ | Weight on childcare: young | -0.10 | Childcare hours: mother | 13 | 12 |
| $\omega^{o}$ | Weight on childcare: old | -0.30 | Childcare hours: grandmother |  |  |
| $p^{n}$ | Childcare price | 4.0 | Mean wage of low-skilled |  |  |

Occupational choice

| $\psi_{2}$ | Training cost: high-skilled | 1.50 | Emp. share of high-skilled | 0.33 | 0.35 |
| :--- | :--- | :---: | :--- | :---: | :---: |
| $\sigma_{e}$ | Std. dev. of shock | 0.10 | $\Delta$ Choice prob. of high-skilled, <br> with child relative to without at age 22 | -0.08 | -0.08 |

Human capital: wage growth by age \& occupation

## Estimation: wage growth moments

Functional specification: $h_{j+1}=(1+\rho(k, n, j)) h_{j}$

$$
\rho(k, n, j)= \begin{cases}\rho_{k, 1}+j \rho_{k, 2} & \text { if } n_{j}=\bar{n} \\ \rho_{k, 0} & \text { if } n_{j}=0\end{cases}
$$

by matching moments of women's wage growth:

| Wage growth per year | High-skilled | Low-skilled |
| :--- | :---: | :---: |
| Employed - Age $\in[25,35]$ | $5.0 \%$ | $2.2 \%$ |
| Employed - Age $\in[40,50]$ | $0.6 \%$ | $0.5 \%$ |
| E-N-E workers | $-8.3 \%$ | $-6.6 \%$ |

[^0]- Parameter values


## Internal parameters: human capital and occupation

| Parameter | Description | Low-skilled | High-skilled |
| :--- | :--- | ---: | ---: |
| $\rho_{k, 1}$ | intrinsic learning speed | 0.025 | 0.055 |
| $\rho_{k, 2}$ | age slope of learning | -0.002 | -0.004 |
| $\rho_{k, 0}$ | depreciation in non-employment | -0.035 | -0.010 |
| $\alpha_{k}$ | occupational wage premium | -0.52 | -0.41 |



Learning speed


Human capital


Wage

## Example : transition of child types

Child transition matrix induced by the fertility process and duration in each bin

| $\pi_{n n^{\prime}}$ | $\pi^{\prime}=1$ | $\pi^{\prime}=2$ | $\pi^{\prime}=3$ | $\pi^{\prime}=4$ | $\pi^{\prime}=5$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\pi=1$ | 0.7024 | 0.2976 | 0 | 0 | 0 |
| $\pi=2$ | 0 | 0.3333 | 0.6667 | 0 | 0 |
| $\pi=3$ | 0 | 0 | 0.3333 | 0.6667 | 0 |
| $\pi=4$ | 0 | 0 | 0 | 0.8 | 0.2 |
| $\pi=5$ | 0 | 0 | 0 | 0 | 1 |

Table: Transition of children number for young generation at age 30

## Model fit: occupational emp. \& wages


(a) Share of high-skilled in emp.

(b) Mean wages

Validation: determinant of young women's labor supply Marginal effects of presence of the old generation

$$
\mathrm{emp}_{i}^{\mathrm{yf}}=\mathbb{1}\left[\alpha_{0}+\alpha_{1} \mathrm{D}_{i}+\alpha^{\prime} \mathbf{X}_{\mathbf{i}}+\epsilon_{i}>0\right]
$$

for women between age 24 and 40

- emp ${ }^{\text {yf }}$ : indicator of employment status of young women
- D: presence of the old generation
- X: controls of linear, quadratic term of experience, and occupation

|  | Model | Data |
| :--- | :---: | :---: |
| All women | 0.040 | 0.066 |
| Women with child | 0.068 | - |
| Women with child under 7 | 0.225 | 0.261 |

Table: Marginal effects of presence of the old generation

## Marginal effect of old: sensitivity

| $\omega_{y}$ | -0.10 <br> Benchmark | -0.05 | -0.15 | -0.2 |  |
| :--- | :--- | :---: | :---: | :---: | :---: |
|  | All women | 0.040 | 0.042 | 0.039 | 0.037 |
|  | All mothers | 0.068 | 0.071 | 0.066 | 0.064 |
|  | With child $<7$ | 0.225 | 0.230 | 0.221 | 0.210 |
| ME of old | -0.30 |  |  |  |  |
|  | $\omega_{o}$ | All women | 0.040 | 0.042 | 0.039 |
|  | All mothers | 0.068 | 0.070 | 0.067 | 0.053 |
|  | With child $<7$ | 0.225 | 0.229 | 0.222 | 0.196 |

## Childcare by employment status

| Age | $\begin{array}{c}\text { Emp. rate } \\ \text { model } \\ \text { data }\end{array}$ | $\begin{array}{c}\text { Hours of employed } \\ \text { model }\end{array}$ |  | $\begin{array}{c}\text { Hours of non-employed } \\ \text { data }\end{array}$ | model |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | $\left.\begin{array}{c}\text { data }\end{array}\right]$| Mothers |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $[25,29]$ | 0.72 | 0.76 | 16.51 | 15.07 | 38.90 | 26.45 |
| $[30,34]$ | 0.67 | 0.82 | 12.53 | 13.95 | 32.50 | 19.86 |
| $[35,39]$ | 0.69 | 0.83 | 10.03 | 9.98 | 28.13 | 15.21 |
| Grandmothers |  |  |  |  |  |  |
| $[50,54]$ | 0.19 | 0.22 | $0.00(0.00)$ | $8.01(0.22)$ | $32.86(0.85)$ | $17.84(0.39)$ |
| $[55,59]$ | 0.09 | 0.10 | $0.00(0.00)$ | $7.67(0.23)$ | $35.00(0.51)$ | $15.00(0.41)$ |
| $[60,64]$ | - | - | - | - | $11.64(0.31)$ | $13.26(0.28)$ |
| $[65,69]$ | - | - | - | - | $15.09(0.29)$ | $9.71(0.18)$ |

## Model fit: childcare hours by children's age

| Age group | Parental hours |  | Non-parental hours |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mother | Father | Total | Grandparents | Market | Total |
| Data |  |  |  |  |  |  |
| Overall | 9.74 | 4.93 |  |  |  |  |
| $[0,2]$ | 15.00 | 6.11 |  |  |  |  |
| $[3,6]$ | 11.79 | 5.47 |  |  |  |  |
| $[7,16]$ | 8.70 | 4.35 |  |  |  |  |
| Model |  |  |  |  |  |  |
| Overall | 17.88 | 9.80 | 2.29 | 13.22 | 3.05 | 42.00 |
| $[0,2]$ | 28.42 | 13.88 | 2.44 | 24.91 | 8.17 | 70.00 |
| $[3,6]$ | 26.60 | 13.65 | 4.29 | 26.82 | 4.12 | 70.00 |
| $[7,16]$ | 8.21 | 5.79 | 0.00 | 0.00 | 0.00 | 14.00 |

Policy Experiment

## Role of age-dependent human capital growth



- lower opportunity cost of non-employment $\rightarrow$ over-predict employment loss at younger ages


## Impact on earnings



Log change

|  |  | Log change |
| :--- | :--- | :---: |
| DPV of | pre-tax wage earnings | $+7.5 \%$ |
|  | after-tax wage earnings | $+12.7 \%$ |
|  | labor earnings | $+4.6 \%$ |

Impact on lifetime earnings

Pre-tax wage earnings by occupation

## Population aging

Reduce death hazard to half of that in the benchmark
$\rightarrow$ increase life expectancy by 2.5 years

|  | Lifetime | By age 40 |
| :--- | :---: | :---: |
| Total working years | $+10.0 \%$ | $-4.9 \%$ |
| Emp. share of high-skilled | $+9.2 \%$ | $+12.5 \%$ |
|  |  |  |
| pre-tax wage earnings | $+2.8 \%$ | $-0.8 \%$ |
| DPV of $\quad$ after-tax wage earnings | $+4.6 \%$ | $+1.0 \%$ |
| $\quad$ labor earnings | $+1.4 \%$ | $+1.0 \%$ |
| Household savings rate | $+5.5 \%$ |  |
| Household welfare | $-0.04 \%$ |  |

Table: Policy effects in the economy of population aging

## Alternative entitlement age

- Consider a set of policy environment: entitlement age between 50 and 60
- Adjust tax and evaluate at the steady state for each entitlement age


Total working years


## Alternative entitlement age

- Consider a set of policy environment: entitlement age between 50 and 60
- Adjust tax and evaluate at the steady state for each entitlement age


Lifetime incomes


Household welfare

## Formal childcare supply

- I specify a reduced-form formal care supply function

$$
p^{n}=\xi_{0}+\xi_{1} Q^{n, s}
$$

with supply elasticity $\frac{1}{\xi_{1}}$.

- Equilibrium achieves when

$$
Q^{n, s}=Q^{n, d}
$$

- Parameter values:
- Benchmark: $\xi_{1}=0$ perfectly elastic formal childcare supply
- No good estimate for China
- United States: $\xi_{1}$ between 1.2 and 1.9
- Conclusion: robust unless childcare supply is extremely inelastic.


## Sensitivity to formal childcare supply elasticity

| Supply elasticity $\frac{1}{\xi_{1}}$ | $\begin{gathered} \infty \\ \text { BM } \end{gathered}$ | 3.0 | 1.2 | 0.5 | 0.1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Childcare price, (log) | 0 | +0.8\% | +1.8\% | +3.8\% | +11.3\% |
| Frac. using grandparental care, (p.p.) | -15.5\% | -15.3\% | -15.0\% | -14.4\% | -12.9\% |
| Frac. using market formal care, (p.p.) | +6.8\% | +6.4\% | +6.0\% | +5.2\% | +3.3\% |
| Choice prob. of high-skilled, (p.p.) | +7.5\% | +7.0\% | +6.7\% | +6.0\% | +3.1\% |
| Total working years | +9.4\% | +9.2\% | +9.0\% | +8.5\% | +7.3\% |
|  | -5.4\% | -5.5\% | -5.7\% | -6.0\% | -6.8\% |
| Lifetime DPV of earnings | +2.5\% | +2.3\% | +2.2\% | +1.6\% | +0.8\% |
|  | +5.4\% | +5.2\% | +5.1\% | +4.8\% | +3.7\% |
|  | +2.2\% | +2.0\% | +1.9\% | +1.9\% | +0.5\% |
| Household savings rate, (p.p.) | +7.1\% | +6.9\% | +6.8\% | +6.7\% | +5.7\% |


[^0]:    4 Back to all moments

