

# How sub-optimal are age-based life-cycle investment products?

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# Overview

## Objective:

- Examine extent to which deterministic age-based life-cycle strategies are ‘near enough’ to optimal
- Two dimensions considered:
  - Glide path, benchmarked against optimal dynamic strategy
  - Risk aversion assumption underpinning the glide path

## Findings:

1. Risk aversion matters – a lot
2. Failing to alter the glide path in response to return realisations also leads to a loss of utility, but it is more moderate
3. Glide path can be improved by basing it on projected balance

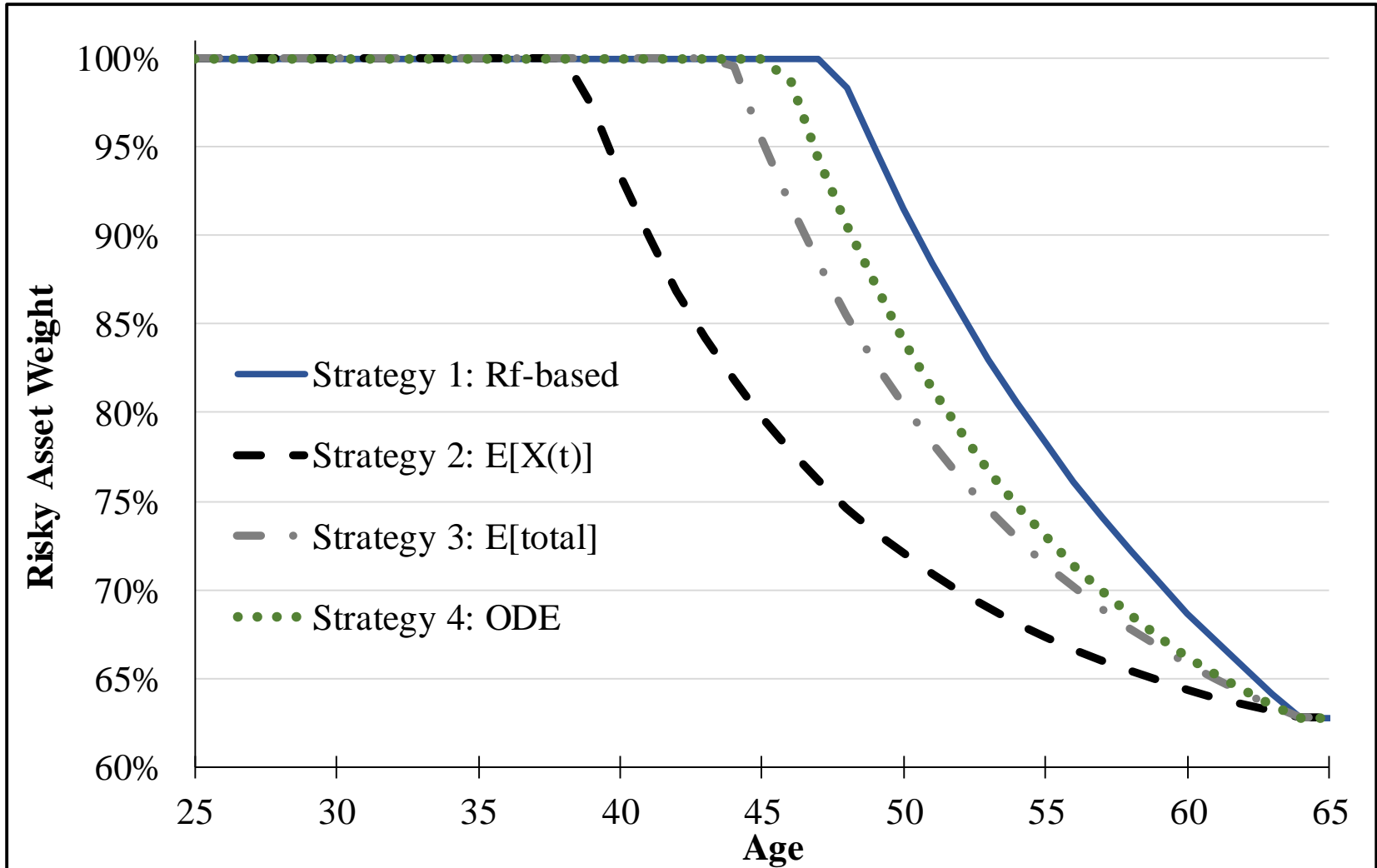
# Strategies examined (1)

Strategy group	Description	Notes
Optimal: dynamic, the benchmark	$\pi(t) = \frac{1}{\gamma} \frac{\alpha - r}{\sigma^2} \frac{X^\pi(t) + h(t)}{X^\pi(t)}$ <p> <math>\alpha, \sigma, r</math> are <math>E(R_e)</math>, <math>SD(R_e)</math>, <math>R_f</math>  <math>\gamma</math> is coefficient of rel. risk aversion (CRRA)  <math>X^\pi(t)</math> is the account balance  <math>h(t)</math> is PV of future contributions </p>	<ul style="list-style-type: none"> <li>• Merton (1971)</li> <li>• Income and hence contributions treated as deterministic</li> <li>• PV of contributions declines over time, implying decrease in risky asset weight</li> </ul>
Proposed strategies	<p>Based on projected balance assuming:</p> <ol style="list-style-type: none"> <li>1. Invests in risk-free asset</li> <li>2. Risky asset return equals its expected value</li> <li>3. Expectation taken of total wealth</li> <li>4. Ordinary differential equation</li> </ol>	<p>All strategies give rise to deterministic glide paths, formed with reference to projection for balance and hence wealth</p>

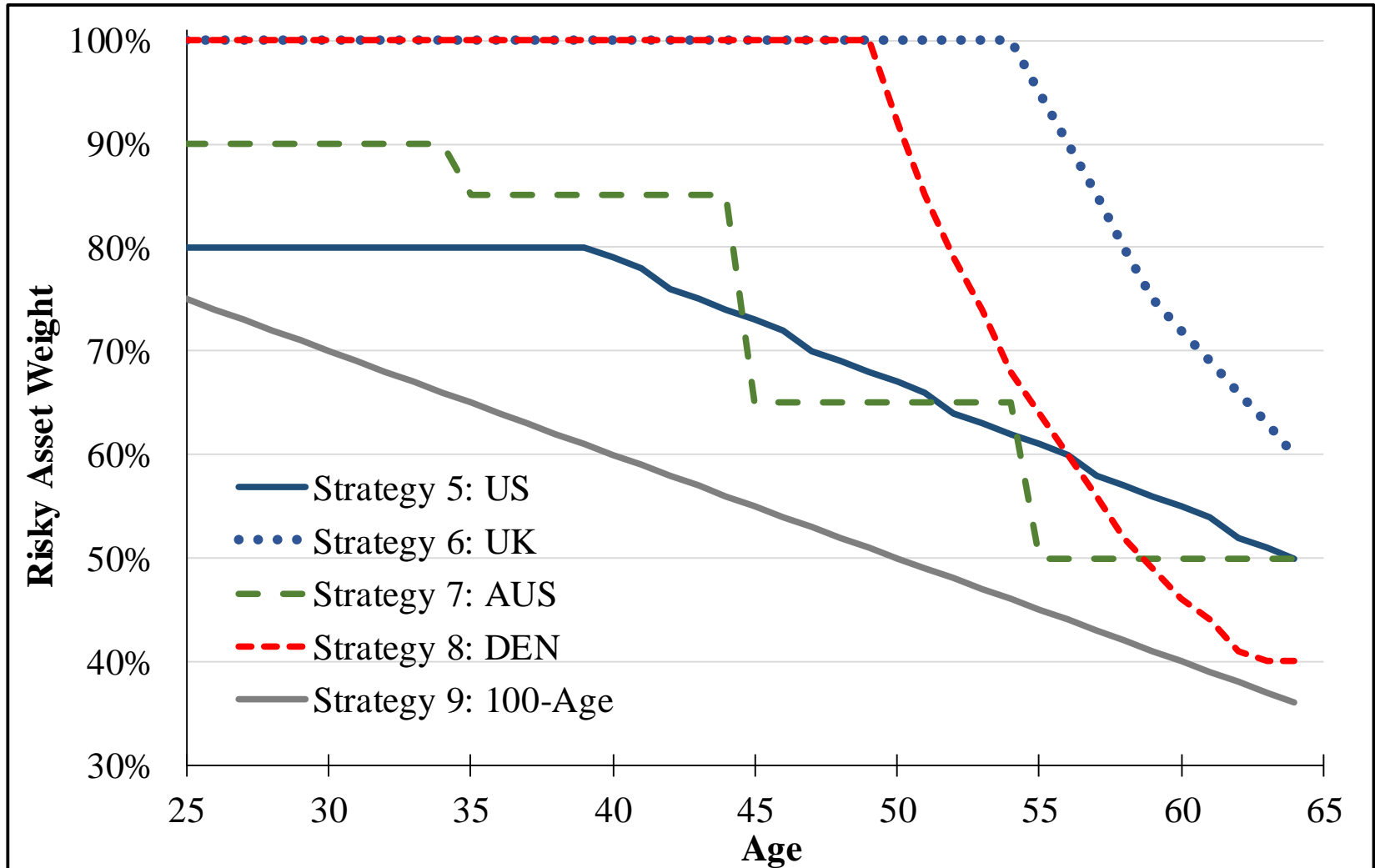
## Strategies examined (2)

Strategy group	Description	Notes
Real life-cycle products	5. US – Vanguard 6. UK – Sky Pension Plan 7. Australia – Commonwealth Super 8. Denmark – PFA plus Pension Plan 9. 100 – Age (rule of thumb)	<ul style="list-style-type: none"> <li>• Variation in glide paths across sample</li> <li>• Ordered by average growth asset weight:               <ol style="list-style-type: none"> <li>a. UK (94%)</li> <li>b. Denmark (85%)</li> <li>c. Australia (73%)</li> <li>d. US (70%)</li> <li>e. Age – 100 (56%)</li> </ol> </li> </ul>
Constant weight strategies	10. Balanced 60/40 11. Risky asset 100% 12. Risk-free asset 100%	Traditional balanced mix, plus the two ‘book-end’ weights

# Glide paths for proposed strategies



# Glide paths for real strategies



# Modelling – A basic set-up

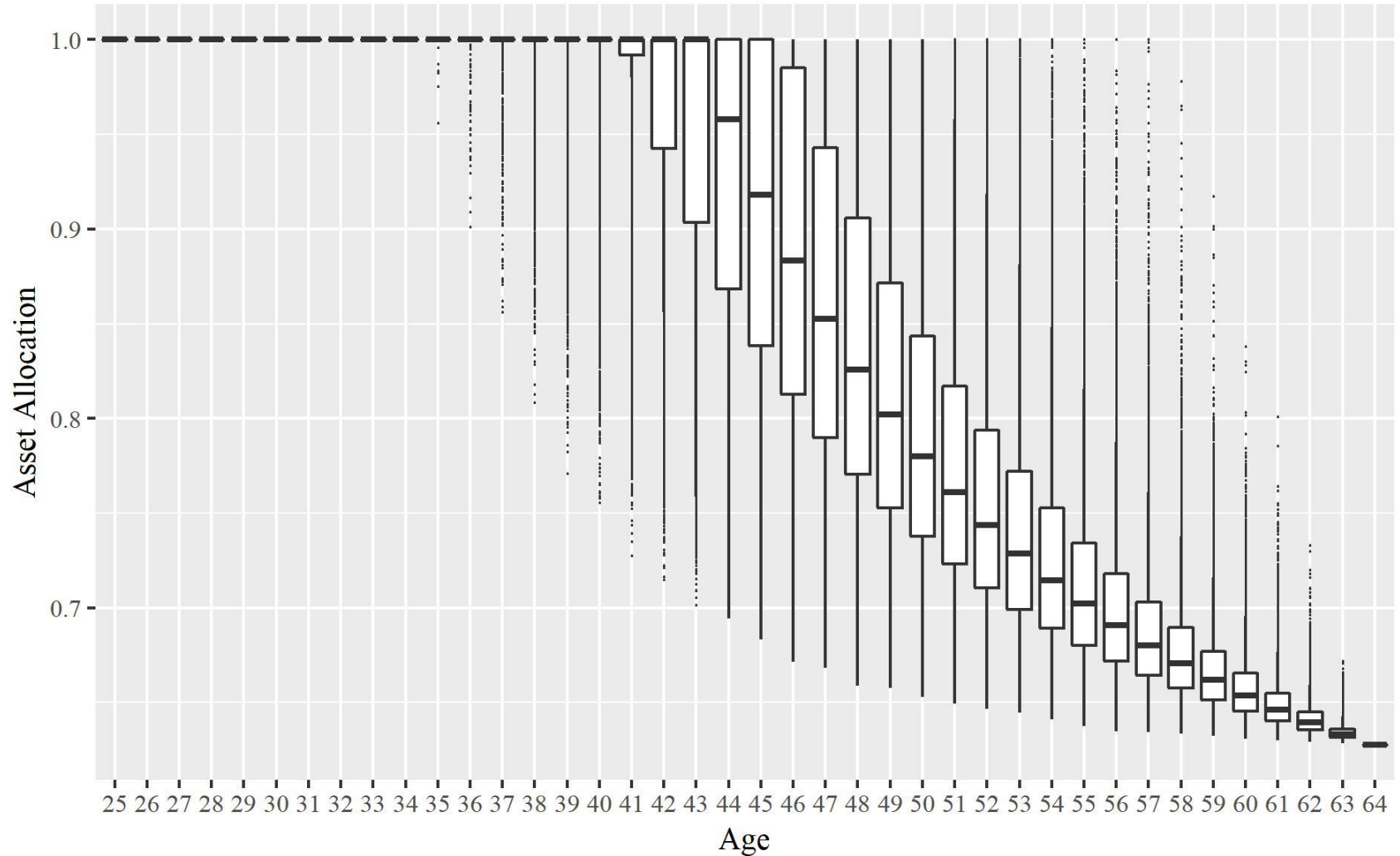
## Assumptions:

- Investor starts working at age 25, retires at age 65
- Constant salary of \$50,000, contribution rate of 10%
- $\alpha = 6.5\%$ ,  $\sigma = 17.4\%$  and  $r = 0.8\%$  (historical real returns)
- No taxes and social security
- Simulate 20,000 asset return paths; numerical approach

## Outcomes and their evaluation:

- Balance at retirement
- Evaluated using power utility function, CRRA range 2 to 5
- Metrics:
  - Summary statistics for distribution of balance at retirement
  - Certainty equivalents – balance at retirement; extra required

# Optimal benchmark strategy (CRRA =3)





# Certainty equivalents – Initial Analysis

*(Optimal – Strategy) / Income = ‘years of income lost’*

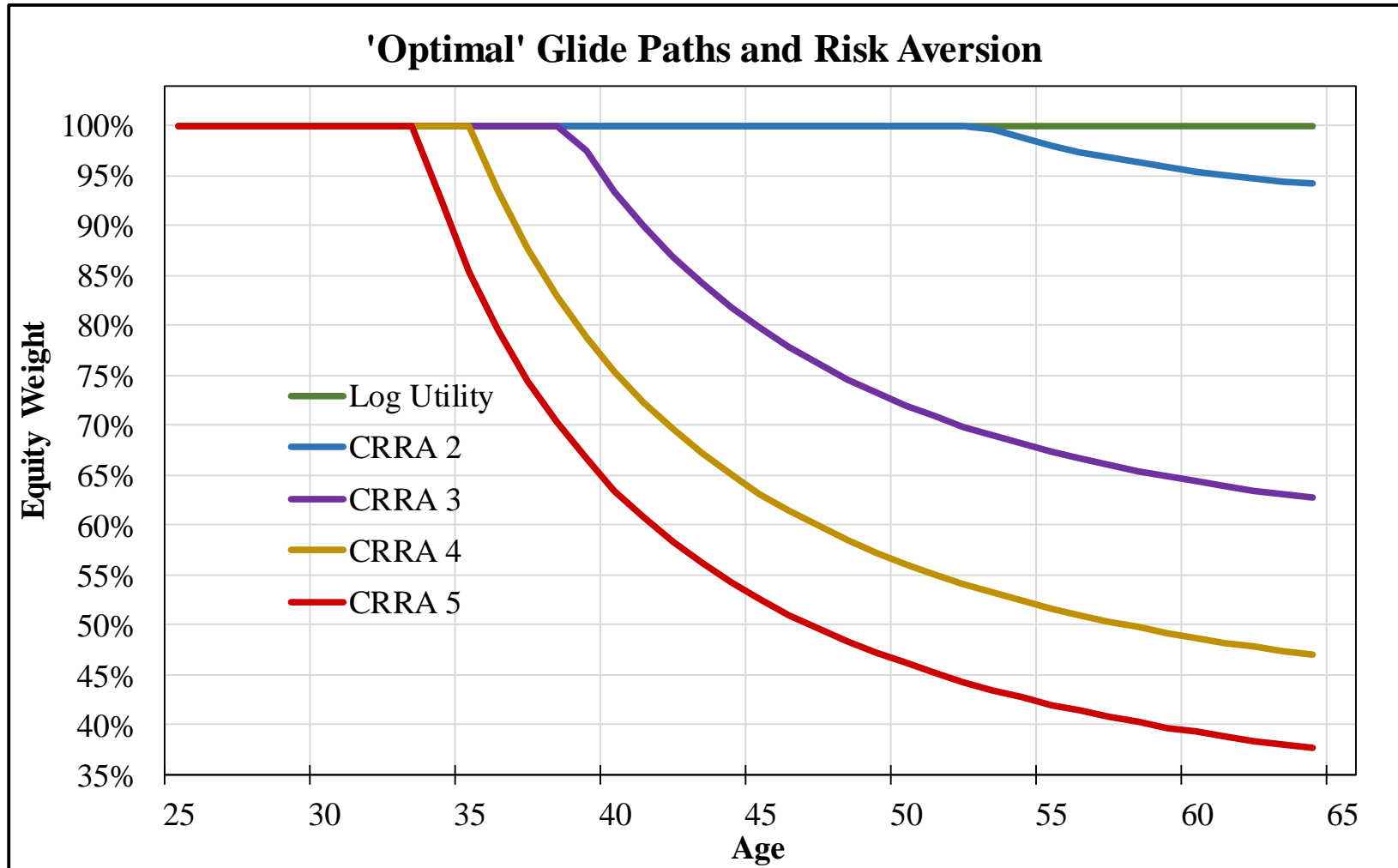
(Optimal - Strategy) / Income		Certainty Equivalent Balance at Retirement				Extra Starting Balance Required			
CRRA:		2	3	4	5	2	3	4	5
<b>Proposed Strategies</b>									
1	Rf-based	0.00	0.04	0.04	0.03	0.00	0.01	0.01	0.01
2	E[X(t)]	0.00	0.07	0.07	0.06	0.00	0.02	0.02	0.02
3	E[total]	0.00	0.02	0.03	0.03	0.00	0.01	0.01	0.01
4	ODE	0.00	0.02	0.03	0.03	0.00	0.01	0.01	0.01
<b>Real Strategies</b>									
5	US	1.32	0.34	0.17	0.27	0.31	0.10	0.06	0.11
6	UK	0.13	0.16	0.63	1.10	0.02	0.05	0.26	0.67
7	AUS	1.29	0.29	0.10	0.19	0.29	0.08	0.04	0.08
8	DEN	0.67	0.13	0.23	0.48	0.14	0.04	0.08	0.24
9	100-Age	2.41	0.93	0.37	0.17	0.67	0.29	0.13	0.07
<b>Constant Weights</b>									
10	60/40	1.88	0.70	0.40	0.41	0.50	0.22	0.14	0.17
11	Risky 100%	0.01	0.49	1.21	1.82	0.00	0.15	0.59	1.43
12	Rf 100%	5.75	3.80	2.80	2.21	4.18	2.76	2.04	1.61

# Certainty equivalents – Proposed strats re-examined

*(Optimal – Strategy) / Income = ‘years of income lost’*

(Optimal - Strategy) / Income		Certainty Equivalent Balance at Retirement				Extra Starting Balance Required			
Evaluated at CRRA of:		2	3	4	5	2	3	4	5
Asset Weights Specified at CRRA = 2		0.00	0.45	1.16	1.75	0.00	0.14	0.55	1.34
		0.00	0.39	1.06	1.65	0.00	0.12	0.49	1.21
		0.00	0.44	1.13	1.73	0.00	0.13	0.54	1.31
		0.00	0.43	1.12	1.71	0.00	0.13	0.53	1.29
Asset Weights Specified at CRRA = 3		0.29	0.04	0.34	0.73	0.06	0.01	0.13	0.39
		0.71	0.07	0.13	0.39	0.15	0.02	0.05	0.18
		0.46	0.02	0.21	0.55	0.09	0.01	0.08	0.27
		0.40	0.02	0.25	0.60	0.08	0.01	0.09	0.30
Asset Weights Specified at CRRA = 4		0.96	0.13	0.04	0.19	0.21	0.04	0.01	0.08
		1.54	0.38	0.07	0.07	0.36	0.11	0.02	0.03
		1.25	0.24	0.03	0.10	0.28	0.07	0.01	0.04
		1.09	0.18	0.03	0.15	0.24	0.05	0.01	0.06
Asset Weights Specified at CRRA = 5		1.63	0.43	0.08	0.03	0.38	0.12	0.03	0.01
		2.19	0.76	0.23	0.06	0.56	0.22	0.08	0.02
		1.93	0.60	0.15	0.03	0.47	0.17	0.05	0.01
		1.94	0.60	0.15	0.03	0.47	0.17	0.05	0.01

# Optimal glide paths and CRRA: A 'level' matter



## Two ‘big’ caveats

1. **Other assets** may significantly alter the solution, in particular:
  - Pension – low-risk, hedging asset
  - Family home – substantial and advantaged asset
2. **Evaluating balance at retirement using power utility** imposes a particular view about member objectives. Other possibilities:
  - Post-retirement outcomes – income, bequest
  - Shorter-term balance as a point of focus
  - Reference dependent utility function

## Conclusions and implications

1. Aligning a product's underlying CRRA assumption with investor risk aversion is CRUCIAL!
  - Utility loss can be substantial if this is out-of-kilter
  - Warning against one-size-fits-all strategies
  - Conservative  $\Rightarrow$  high growth options are offered in the 'balanced' fund arena. Why not the same in life-cycle?
2. Applying a deterministic rather than dynamic glide path can also lead to utility loss, but it is more moderate.
3. Scope exists for improving the design of deterministic life-cycle strategies by applying one of our proposed strategies.

***Questions?***

***Discussion?***